



# Advanced Control of Twin Rotor MIMO system

Kannan P S

Department of Electrical and Electronics Engineering  
Mar Baselios College of Engineering and Technology  
Kerala, India  
kannanps17@gmail.com

Sheenu P

Department of Electrical and Electronics Engineering  
Mar Baselios College of Engineering and Technology  
Kerala, India  
george.sheenu@gmail.com

**Abstract**— Control design of a multiple input system such as helicopter is very challenging task. This is because of the high non-linearity, significant cross-coupling and inaccessibility of some of its states and outputs for measurements. MIMO control design has been explored in the laboratory with the help of Twin Rotor MIMO system (TRMS). A Twin rotor MIMO system consists of two rotors called main rotor and tail rotor. These two rotors are situated on a beam, supported by a counter balance. Two degrees of freedom (DOF) dynamic model of the TRMS involving pitch and yaw motion was obtained for controller design. PID controllers were designed for TRMS by pole placement method using root locus technique for some desired specifications in which we have considered the performance specifications as settling time equal to 4 seconds and percentage overshoot less than 25%. The root locus of the closed loop system ensured that even if the gain K value was increased, the root locus of the closed loop system remained in the stable region. Thus, the tracking error of the TRMS model was reduced to less than 1% with the help of properly designed PID controllers. The study of Eigen Structure Assignment and Relative Gain Array algorithm methods were conducted and are now to be implemented to the TRMS model which is considered. A comparative study of the three methods is to be carried out, which is included as future work.

**Index Terms**—, PID controller, parameter variations, uncertainties, Twin Rotor MIMO systems(TRMS).

## I. INTRODUCTION

TWIN ROTOR MIMO system consists of two rotors called main rotor and tail rotor. These two rotors are situated on a beam together with a counterbalance as shown in Fig.1.1. The main rotor is free to rotate in the horizontal plane in which angle of rotation is called pitch and the tail rotor is free to rotate in the vertical plane in which angle of rotation is called yaw. The twin rotor system is equivalent to a helicopter in certain aspects. This system has two degree of freedom (2-DOF) on pitch and yaw angles. Twin rotor system attracts control engineers and researchers because it has the presence of uncertainty, complexity, parameter variations, and external disturbances. In recent years, a lot of approaches have been devised for the control of twin rotor system. An adaptive second order sliding mode (SOSM) controller is proposed to

control a laboratory helicopter twin rotor MIMO system (TRMS) [1]. The decoupling control of a TRMS is studied and proposed to apply robust deadbeat control technique to this nonlinear system [2].

A decoupled compensator has been designed for a physical TRMS system [3]. For control of TRMS with 2-DOF, a modified real-value-type genetic algorithm (RGA) for tuning the parameters of the proportional integral derivative (PID) controller is used [4]. A fuzzy sliding and fuzzy integral sliding controller (FSFISC) is designed to position the yaw and pitch angles of the TRMS system [5]. A fuzzy PID technique with RGA to control a TRMS has been discussed. A TRMS is decoupled and fuzzy Takagi-Sugeno (T-S) model of TRMS is obtained [7]. On the basis of T-S model, a parallel distributed fuzzy linear quadratic regulator (LQR) controller is designed to control the position of the pitch and yaw angles. Implementation of an adaptive dynamic nonlinear model inversion control law for a TRMS using artificial neural networks (ANN) has been discussed [8].

An observer for nonlinear TRMS has been implemented in [9]. The nonlinearities which are unknown are estimated by Chebyshev neural network whose weights are adaptively adjusted. A quasi-linear parameter varying (quasi-LPV) modeling, identification and control of a TRMS is presented [10]. A twin rotor system is modeled using an ant colony optimization (ACO) technique [11]. A robust adaptive tracking control scheme is developed using back-stepping technique and the dynamic surface control method for a nonlinear MIMO system [12].

Even though greater advancement techniques have been arrived for finding the stability of TRMS, they won't give exact results according to the way in which we design. ie, we want the system to satisfy certain performance specifications which we assign. This paper is aimed at designing a controller for compensating the parameter variations and external disturbances existing in both pitch and yaw motion of a TRMS. The trajectory tracking controller proposed in this paper uses a PID controller, which is obtained by pole

placement technique, satisfying the desired performance specifications. A state feedback control law is also to be implemented using Eigen structure assignment [13] so that the desired poles will be the eigen values of the closed loop system. Now these results are to be compared with the Relative Gain Array approach[14]. Here the pole placement technique using root locus has been explained, by modeling the linear system of TRMS. [6] proposed a principle in which another NN yield input control law was created for an under incited quad rotor UAV which uses the regular limitations of the under incited framework to create virtual control contributions to ensure the UAV tracks a craved direction. Utilizing the versatile back venturing method, every one of the six DOF are effectively followed utilizing just four control inputs while within the sight of un demonstrated flow and limited unsettling influences.

A comparison between the non-linear model and the linear one has been done and the responses were compared both for the open loop and closed loop system.

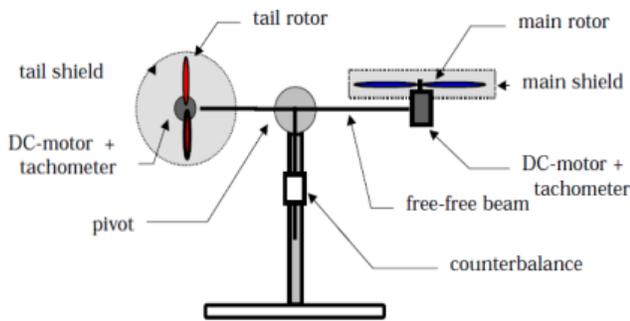


Fig. 1.1 Aero-dynamical model of TRMS

The simulations were conducted in Matlab by providing step input of unity as the inputs to two rotors. The responses of the pitch and yaw motion of the two rotors were compared for both linear as well as non-linear systems.

The outline of this paper is as follows. Section II is the model description of TRMS; Section III involves the design and simulation of PID controllers for both the rotors. Concluding remarks are given in Section IV.

## II. MODEL DESCRIPTION

TRMS consists of two propellers which are perpendicular to each other and joined by a beam pivoted on its base. The system can rotate freely in both vertical and horizontal direction. Both propellers are driven by DC motor and by changing the voltage supplied to beam, rotational speed of propellers can be controlled. For balancing the beam in steady state, counterweight is connected to the system. Both propellers are shielded so that the environmental effects can be minimized. The complete unit is attached to the tower which

ensures safe helicopter control experiments. The electrical unit is placed under the tower which is responsible for communication between TRMS and PC. The electrical unit is responsible for transfer of measured signal by sensors to PC and transfer of control signal via I/O card. Main rotor is responsible for controlling the flight of TRMS in vertical direction and Tail rotor is responsible for controlling the flight of TRMS in horizontal direction.

The mathematical model derived from phenomenological model shown in Fig 2.1 is nonlinear in nature that means at least one of the states (rotor current or position) is an argument of non-linear function. In order to design the controller for controlling the flight of TRMS, the mathematical model should be linearized. According to model represented in Fig1.2, the non-linear mathematical model of TRMS are formed and are shown below:

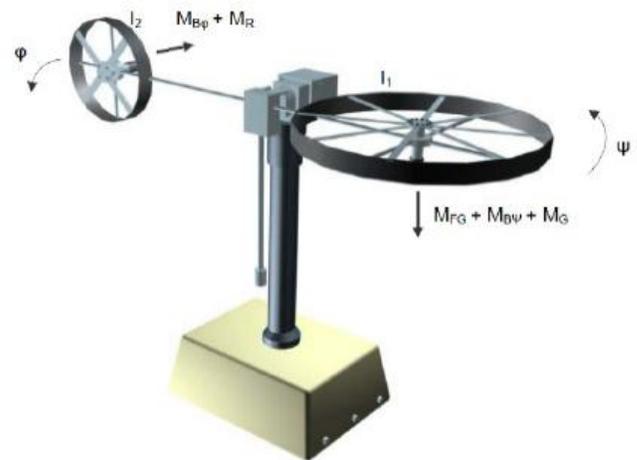


Fig. 2.1 Mechanical-Electrical model of TRMS

Mathematical equation in vertical plane is given by:

$$\begin{aligned}
 I_1 \ddot{\psi} &= M_1 - M_{FG} - M_{B\psi} - M_G \\
 M_1 &= a_1 \tau_1^2 + b_1 \tau_1 \\
 M_{FG} &= M_g \sin \psi \\
 M_{B\psi} &= B_1 \dot{\psi} + B_2 \psi \text{sign}(\dot{\psi}) \\
 M_G &= K_{gy} M_1 \dot{\psi} \cos(\psi)
 \end{aligned}
 \tag{1}$$

Where  $M_1$  is the non-linear static characteristics,  $M_G$  is the gyroscopic momentum and  $M_{FG}$  is the gravity momentum.

The motor and the electrical control circuit is approximated as a first order transfer function, thus the main rotor momentum in Laplace domain is described as-



$$\tau_1 = \frac{k_1}{T_{11}s + T_{10}} u_1 \quad (2)$$

Mathematical equation in horizontal plane is given as-

$$\begin{aligned} I_2 \ddot{\phi} &= M_2 - M_{B\phi} - M_R \\ M_2 &= a_2 \tau_2^2 + b_2 \tau_2 \\ M_{B\phi} &= B_{1\phi} \dot{\phi} + B_{2\phi} \text{sign}(\dot{\phi}) \\ M_R &= \frac{k_c (T_0 s + 1)}{(T_p s + 1)} \tau_1 \end{aligned} \quad (3)$$

Where  $M_R$  is the cross reaction momentum, and the tail rotor momentum in Laplace domain is given as-

$$\tau_2 = \frac{k_2}{T_{21}s + T_{20}} u_2 \quad (4)$$

TABLE I  
 NOMINAL PARAMETERS OF A TRMS

PARAMETER	VALUE
$I_1$ – momemt of inertia of vertical rotor	$6.8 \cdot 10^{-2} \text{ kg.m}^2$
$I_2$ – momemt of inertia of horizontall rotor	$2.10 \cdot 10^{-2} \text{ kg.m}^2$
$a_1$ – static characteristic parameter	0.0135
$b_1$ – static characteristic parameter	0.0924
$a_2$ – static characteristic parameter	0.02
$b_2$ – static characteristic parameter	0.09
$M_g$ – gravity momentum	0.32N.m
$B_{1\psi}$ – friction momentum function parameter	$6.10 \cdot 10^{-3} \text{ N.m.s / rad}$
$B_{2\psi}$ – friction momentum function parameter	$1.10 \cdot 10^{-3} \text{ N.m.s}^2 / \text{ rad}$

$B_{1\phi}$ – friction momentum function parameter	$1.10 \cdot 10^{-1} \text{ N.m.s / rad}$
$B_{2\phi}$ – friction momentum function parameter	$1.10 \cdot 10^{-2} \text{ N.m.s}^2 / \text{ rad}$
$K_{gy}$ – gryoscopic momentum parameter	$0.05 \text{ s / rad}$
$k_1$ – motor 1 gain	1.1
$k_2$ – motor 2 gain	0.8
$T_{11}$ – motor 1 deno parameter	1.1
$T_{10}$ – motor 1 deno parameter	1
$T_{21}$ – motor 2 deno parameter	1
$T_{20}$ – motor 2 deno parameter	1
$T_p$ – cross reaction momentum parameter	2
$T_0$ – cross reaction momentum parameter	3.5
$k_c$ – cross reaction momentum gain	-0.2

The table I gives the approximate values of parameters.

### A. State-Space Representation

By using the dynamical equations, the state space model of the linearised plant is given by

$$\dot{x} = Ax + Bu \quad (5)$$

$$y = Cx + Du$$

The State vector is:

$$x = [\psi \ \dot{\psi} \ \phi \ \dot{\phi} \ M_R \ \tau_1 \ \tau_2]^T \quad (6)$$

The input vector is:

$$u = [u_1 \ u_2]^T \quad (7)$$

The output vector is:

$$y = [\psi \ \phi]^T \quad (8)$$

Output matrix as:

$$C = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 \end{bmatrix}$$

$$A = \begin{bmatrix} 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ \frac{-M_x}{I_1} & \frac{-B_w}{I_1} & 0 & 0 & 0 & \frac{b_1}{I_1} & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{-B_y}{I_2} & \frac{-1}{I_2} & 0 & \frac{b_2}{I_2} \\ 0 & 0 & 0 & 0 & \frac{-1}{T_p} & \frac{k_x}{T_p} \left( \frac{-T_{10}}{T_{11}} T_0 + 1 \right) & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{-T_{10}}{T_{11}} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & \frac{-T_{20}}{T_{11}} \end{bmatrix}$$

### B. Transfer Function Model

The transfer function model of the TRMS is obtained by converting the state-space model into equivalent transfer function by using Matlab commands. Thus we get two transfer functions representing the pitch and yaw rotors as given below:

Pitch rotor transfer function:

$$G_p = \frac{1.359}{s^3 + 0.997s^2 + 4.786s + 4.278} \quad (9)$$

Yaw rotor transfer function:

$$G_y = \frac{3.6}{s^3 + 6s^2 + 5s} \quad (10)$$

Four transfer functions are obtained, out of which two of them are formed due to the significant cross coupling between the two rotors. We are not much bothered about the remaining transfer functions, since we decoupling the MIMO system into two SISO models, and designing the controllers separately.

$$B = \begin{bmatrix} 0 & 0 \\ 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ \frac{k_1}{T_{11}} \frac{k_c}{D_F} \begin{bmatrix} T_0 & 0 \\ 0 & 0 \end{bmatrix} & 0 & 0 & 0 & 0 & 0 & 0 \\ \frac{k_1}{T_{11}} & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & \frac{k_2}{T_{21}} & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

By substituting the values given in the table for the A,B,C and D matrices, we obtain the values as given below:

State Transition Matrix as:

$$A = \begin{bmatrix} 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ -47059 & -0088 & 0 & 0 & 0 & 1.359 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & -5 & -50 & 0 & 45 \\ 0 & 0 & 0 & 0 & -0.5 & 0.22 & 0 \\ 0 & 0 & 0 & 0 & 0 & -0.909 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -1 \end{bmatrix}$$

Input matrix as :

$$B = \begin{bmatrix} 0 & 0 \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \\ -0.35 & 0 \\ 1 & 0 \\ 0 & 0.8 \end{bmatrix}$$

### III. DESIGN OF PID CONTROLLERS

In this section, we are dealing with the design of PID controllers by means of pole placement technique. Before going deep into the controller design part we shall first discuss about the technique using root locus approach. In pole placement technique, we are placing the poles of the system in such a way that the root locus of the closed loop system will pass through the desired pole location, that we have selected by meeting some of the performance specifications. Here we are selecting the performance specifications as settling time equal to 4seconds and percentage overshoot equal to 25%. Thus we get the natural frequency of oscillation  $\omega_n = 2.4471 \text{ rad / sec}$  and damping coefficient  $\varepsilon = 0.403$ .

By plotting the root locus of the open loop system, we found that system is stable for only for some range of K. As the value of K is increased the root locus will move in to the right half of s-plane, ie. towards the unstable region. We are designing a controller such that, poles are placed according to the design specification and shape of root locus is changed so that it passes through the desired pole location. For the yaw



rotor, it is obtained by the addition of zero on the negative real axis, after fixing the poles. With the addition of zero itself we have made the system stable, by adjusting the position of zero along the negative real axis. By doing the procedure, we have to make sure about the root locus shape whether it is passing through the desired poles. For the sake of convenience we shall discuss how the method is implemented for the yaw rotor.

### A. Pole Placement Technique

Let us consider the root locus of the open loop transfer function of yaw rotor.

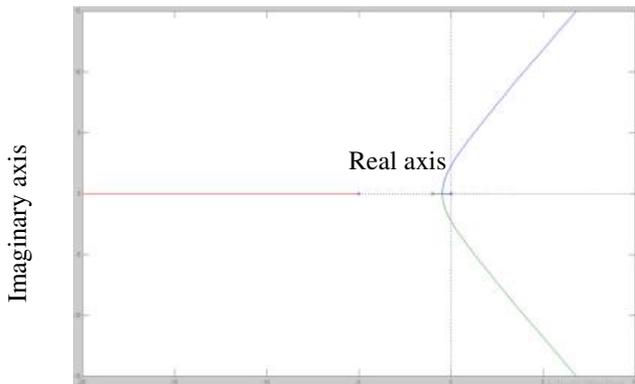


Fig. 3.1 Root locus of the open loop transfer function of Yaw rotor.

The open loop plant is stable for only some value of  $K$ , so in order to make the plant globally stable, we design PID controller values by meeting the performance specifications mentioned earlier. Here first we fix the desired poles as shown in Fig 3.2

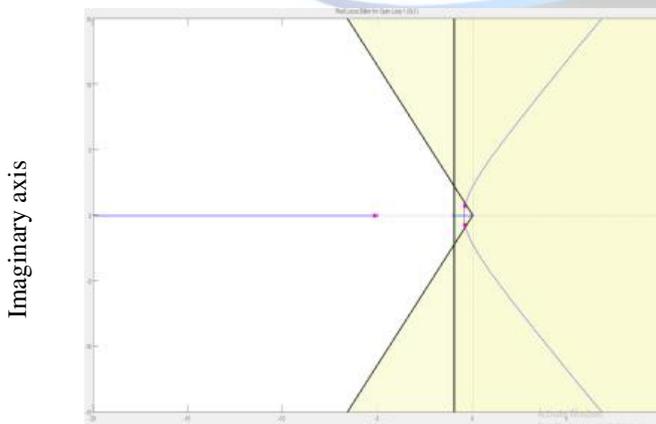


Fig. 3.2 Fixing the desired pole location for the system

Now the shape of the root locus is changed by the addition of zero on the negative real axis as show in Fig 3.3.

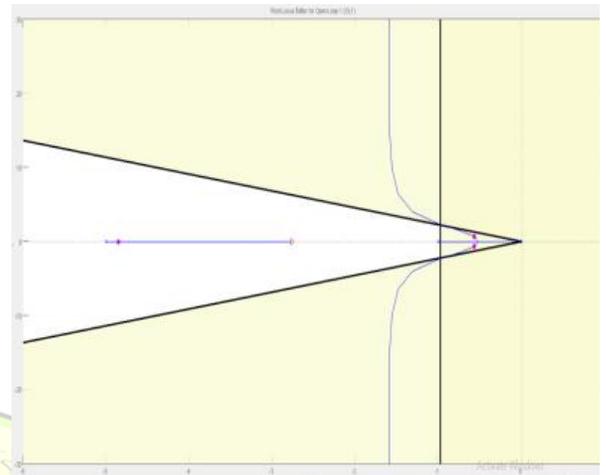


Fig. 3.3 Changing the shape of root locus by addition of zero

Here  $K_p$  value is obtained as the overall gain of the closed loop system i.e.,  $K_p = 6.73$ .

For the ideal case, PID controller combination is taken as form, ie,

$$G_c = K_p \left( 1 + K_d s + \frac{K_i}{s} \right) \quad (11)$$

We are not introducing any pole to the system, so  $K_i$  value is equal to 0. Then equating the above equation to zero, we get the value of  $K_d = 0.3663$ .

In the same way PID controller is designed for the Pitch rotor also.

TABLE II  
 VALUES OF P, I & D FOR THE ROTORS

Rotor type	$K_p$	$K_i$	$K_d$
Pitch	0.0134	53.44	11.37
Yaw	6.73	0	0.366

From Table II we can see that only PD controller was sufficient to stabilize the Yaw rotor, but for the Pitch rotor, due to the presence of complex zeros we required PID controller to make the system stable.

### B. Block diagram representation

After successful modeling and design of PID controllers for the TRMS, we need to compare the results of both linear as well as the non linear system, whether they are showing similar response towards a step input applied to them. For that we use the following block diagram.

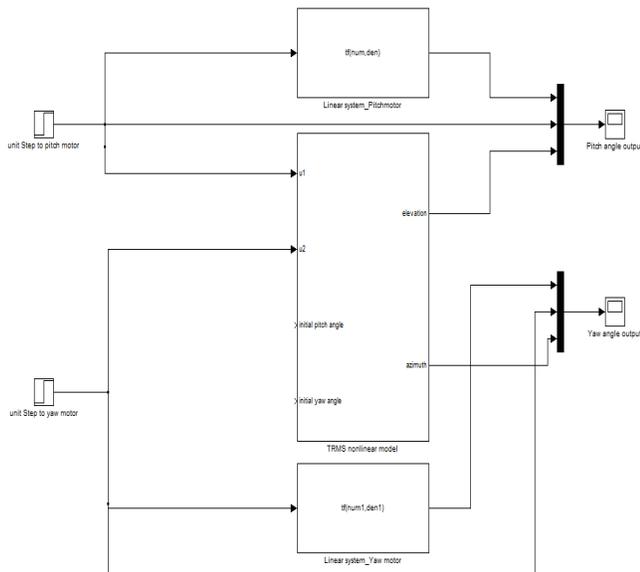


Fig. 3.4 Combined block diagram for the linear and non-linear system without controller.

Combined linear and non-linear block diagram representation of TRMS is shown in Fig 3.4. This is the open loop block diagram, and the responses shown that both linear

and the non-linear systems are having similar open loop characteristics. Now we need to confirm the similarity in the closed loop case, by satisfying the performance specifications.

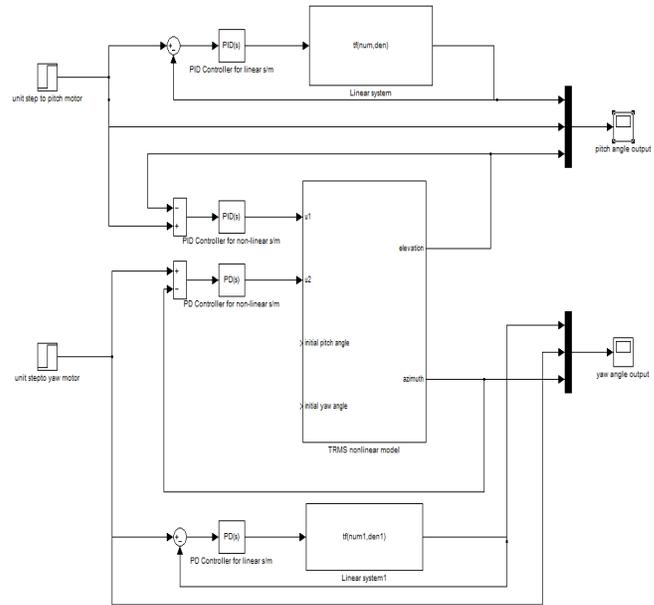


Fig. 3.5 Combined block diagram for the linear and non-linear system with PID controller.

The comparison of closed loop system was also done successfully i.e., the closed loop systems of the pitch and yaw rotor for both linear and non-linear systems are showing similar responses satisfying the defined performance specifications.

## IV. SIMULATION RESULTS

A Twin Rotor MIMO System was modeled and pole placement method using root locus technique was used to design PID controllers and applied to the Simulink model of the system. All the simulations were carried out in Matlab Simulink. Step input was given as the references for both pitch and yaw rotors to study the response of PID controllers.

### A. Response of open loop system

The open loop response of both the pitch and yaw rotors are shown in figure 4.1. we can see that both are showing the same characteristics. The following figure shows the open loop response. Here the yellow line represents the linear system of TRMS which we have designed by eliminating the non-linearities and the blue line represents the response of the non-linear system of TRMS. In the open loop, by providing a step input to the systems, they are showing stable but not tacking to the step value. Here we have given a step input of unity. Thus, we go for the closed loop system using PID

controllers to reduce the tracking error by satisfying the performance specifications.

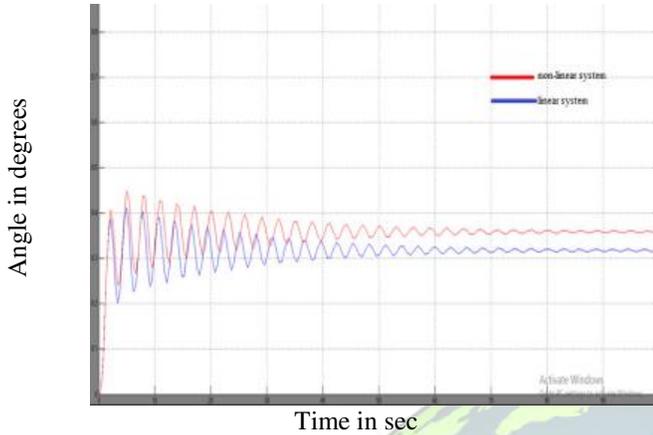
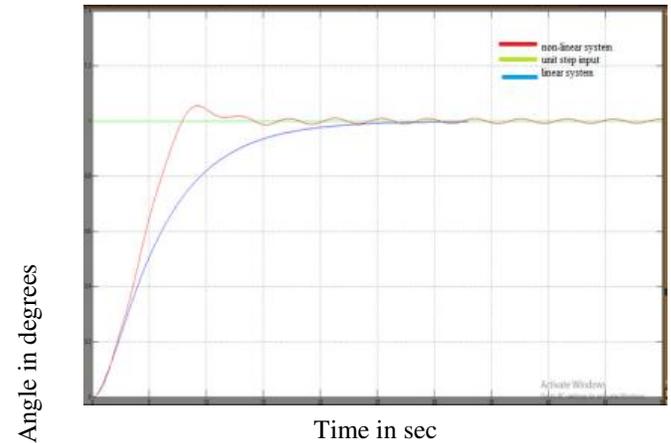


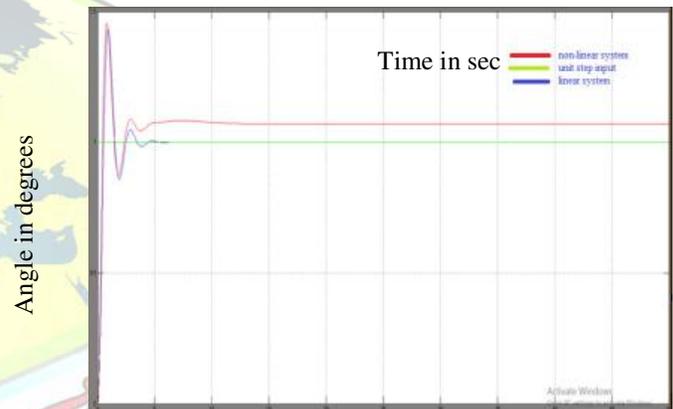
Fig. 4.1 Response of both systems towards a unit step input

### B. Response of closed loop system

The response of the closed loop system given in figures 4.2 (a) and 4.2 (b) shows that both the pitch and yaw rotors are tracking the step input given to it. We have designed the PID controller such that the settling time is less than 4seconds and the overshoot is about 25%. The response is showing only a small difference from the specifications that we have mentioned, ie an error of 0.01%, which is less than 1%. Here we can see that the response of yaw rotor is satisfactory as compared to that of the pitch rotor, this is because, the transfer function of pitch rotor is more complex as compared to that of the yaw rotor, where the addition of zero gave the desired response. But for the pitch rotor, due to the presence of complex poles, complex zeros were added to cancel out the poles. And so the P,I,D values are obtained such as to cancel out the denominator terms. Thus our closed loop system is stable, and tracking errors are reduced to less than 1%.



(a) Response of pitch rotor



(b) Response of yaw rotor

Fig. 4.2 Response of both systems towards a unit step input with PID controllers.

Thus our system is now ready to be implemented for future control techniques such as Eigen Structure Assignment and Relative Gain Array algorithm techniques, which are selected as the future extension of the work.

### V. CONCLUSIONS

A Twin Rotor MIMO system was modeled by considering 7 states. There are two inputs and two outputs for the TRMS, so it is a MIMO system having two degrees of freedom along the pitch and yaw angles of motion. PID controllers were designed for TRMS using pole placement method by root locus technique for desired specifications in which we have considered the performance specification as settling time equal to 4 seconds and percentage overshoot less than 25%. The root locus of the closed loop system ensured that even if the gain K value was increased, the root locus remained in the stable region. Thus, the tracking error of the closed loop system were reduced to less than 1% with the help of properly designed PID controllers for both linear as well as for the non-linear system of TRMS. The open loop and closed loop responses of



**International Journal of Advanced Research Trends in Engineering and Technology (IJARTET)**  
**Vol. 4, Special Issue 6, April 2017**

both the systems were then compared and ensured the similarity in their responses. Now it is able to implement techniques of Eigen structure Assignment and RGA algorithm to the TRMS model that we have considered.

**REFERENCES**

- [1] S. Mondal and C. Mahanta, "Adaptive second-order sliding mode controller for a twin rotor multi-input-multi-output system," *IET Control Theory Appl.*, vol. 6, no. 14, pp. 2157-2167, 2012.
- [2] P. Wen and T. W. Lu, "Decoupling control of a twin rotor MIMO system using robust deadbeat control technique," *IET Control Theory Appl.*, vol. 2, no. 11, pp. 999-1007, 2008.
- [3] J. K. Pradhan and A. Ghosh, "Design and implementation of decoupled compensation for a twin rotor multiple-input and multiple-output system," *IET Control Theory Appl.*, vol. 7, no. 2, pp. 282-289, 2013.
- [4] J. G. Juang, M. T. Huang, and W.-K. Liu, "PID control using presearched genetic algorithms for a MIMO system," *IEEE Transactions on Systems, Man, and Cybernetics-Part C: Applications and Reviews*, vol. 38, no. 5, pp. 716-727, 2008.
- [5] C. W. Tao, J. S. Taur, Y. H. Chang, and C. W. Chang, "A Novel Fuzzy-Sliding and Fuzzy-Integral-Sliding Controller for the TwinRotor Multi-Input-Multi-Output System," *IEEE Transactions on Fuzzy Systems*, vol. 18, no. 5, pp. 893-905, 2010.
- [6] Christo Ananth, "A NOVEL NN OUTPUT FEEDBACK CONTROL LAW FOR QUAD ROTOR UAV", *International Journal of Advanced Research in Innovative Discoveries in Engineering and Applications [IJARIDEA]*, Volume 2, Issue 1, February 2017, pp:18-26.
- [7] Liu, H., Lu, G., Zhong, Y.: 'Robust LQR attitude control of a 3- DOF laboratory helicopter for aggressive maneuvers', *IEEE Trans. Ind. Electron.*, 2013, 60, (10), pp. 4627-4636
- [8] Liu, C., Chen, W.-H., Adrews, J.: 'Tracking control of small-scale helicopters using explicit nonlinear MPC augmented with disturbance observers', *Control Eng. Pract.*, 2012, 20, (3), pp. 258-268
- [9] Kiefer, T., Graichen, K., Kugi, A.: 'Trajectory tracking of a 3DOF laboratory helicopter under input and state constraints', *IEEE Trans. Control Syst. Technol.*, 2010, 18, (4), pp.
- [10] Apkarian, J.: '3-DOF helicopter reference manual' (Quanser Consulting Inc, Canada, 2006)
- [11] Kutay, A.T., Calise, A.J., Idan, M., Hovakimyan, N.: 'Experimental results on adaptive output feedback control using a laboratory model helicopter', *IEEE Trans. Control Syst. Technol.*, 2005, 13, (2), pp. 196-202
- [12] Andrievsky, B., Peaucelle, D., Fradkov, A.L.: 'Adaptive control of 3DOF motion for LAAS helicopter benchmark: design and experiments'. Proc. American Control Conf., New York, USA, July 2007, pp. 3312-3317
- [13] Rahideh, M.H. Shaheed and H.J.C. Huijberts. "Dynamic Modelling of the TRMS using Analytical and Empirical approaches", *Control Engineering Practice*, Volume 16, Issue 3, March 2008, Pages 241-259.
- [14] Feedback Instruments Ltd, Twin Rotor MIMO System Control Experiments, 33-949S, Laboratory Manual.
- [15] Youdan Kim and Hen-Seob Kim, "Eigen Structure Assignment Algorithm for Mechanical systems", *J Guidance* vol.22.No 5.
- [16] T.K Liu and Juang: "A Single Neuron PID Control for Twin Rotor MIMO System", *IEEE/ASME International Conference on Advanced Intelligent Mechatronics*, , 2009.
- [17] Lih-Gau luang, Wen-Kai Liu, Cheng-Yu Tsai, "Intelligent Control Scheme for Twin Rotor MIMO System", *Proceedings of the 2005 IEEE International Conference on Mechatronics* July 10-12. 2005, Taipei, Taiwan.
- [18] M. L. Kerr, S. Jayasuriya, S. F. Asokanathan, "QFT based robust control of a single link flexible manipulator," *Journal of Vibration and Control*, vol. 13, no. 1, pp. 3-27, 2007.
- [19] S. M. M. Alavi, M. J. Walsh, and M. J. Hayes, "Robust distributed active power control technique for IEEE 802.15.4 wireless sensor networks-A quantitative feedback theory approach," *Control Engineering Practice*, vol. 17, pp. 805-814, 2009.
- [20] F. Chen, B. Jiang, and C. Jiang, "Self-repairing control for UAVs via quantitative feedback theory and quantum control techniques," *Procedia Engineering*, vol. 15, pp.1160-1165,2011.
- [21] S. F. Wu, and D. Fertin, "Spacecraft drag-free attitude control system design with quantitative feedback theory," *Acta Astronautica*, vol. 62, pp. 668-682, 2008.